1	JOINT for Large-scale Single-cell RNA-Sequencing Analysis via Soft-clustering and
2	Parallel Computing
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#### 17 ABSTRACT

#### 18 Background

Single-cell RNA-Sequencing (scRNA-Seq) has provided single-cell level insights into complex biological processes. However, the high frequency of gene expression detection failures in scRNA-Seq data make it challenging to achieve reliable identification of cell-types and Differentially Expressed Genes (DEG). Moreover, with the explosive growth of single-cell data using 10x genomics protocol, existing methods will soon reach the computation limit due to scalability issues. The single-cell transcriptomics field desperately need new tools and framework to facilitate large-scale single-cell analysis.

#### 26 **Results**

27 In order to improve the accuracy, robustness, and speed of scRNA-Seq data processing, we propose a generalized zero-inflated negative binomial mixture model, "JOINT," that can perform 28 29 probability-based cell-type discovery and DEG analysis simultaneously without the need for imputation. JOINT performs soft-clustering for cell-type identification by computing the 30 probability of individual cells, i.e. each cell can belong to multiple cell types with different 31 probabilities. This is drastically different from existing hard-clustering methods where each cell 32 can only belong to one cell type. The soft-clustering component of the algorithm significantly 33 facilitates the accuracy and robustness of single-cell analysis, especially when the scRNA-Seq 34 35 datasets are noisy and contain a large number of dropout events. Moreover, JOINT is able to determine the optimal number of cell-types automatically rather than specifying it empirically. 36 The proposed model is an unsupervised learning problem which is solved by using the 37 38 Expectation and Maximization (EM) algorithm. The EM algorithm is implemented using the

-2-

39 TensorFlow deep learning framework, dramatically accelerating the speed for data analysis40 through parallel GPU computing.

41 Conclusions

42 Taken together, the JOINT algorithm is accurate and efficient for large-scale scRNA-Seq data

43 analysis via parallel computing. The Python package that we have developed can be readily

44 applied to aid future advances in parallel computing-based single-cell algorithms and research in

45 various biological and biomedical fields.

46

#### 47 **KEYWORDS**:

48 RNA-Seq; Single-cell; Dropout; JOINT; Deep Learning; Probability; Soft-clustering; DEG;
49 Parallel Computing

50

#### 51 BACKGROUND

scRNA-Seq technology has significantly advanced the understanding of human disease and 52 underlying biological processes at the single-cell level [1, 2]. This ever-evolving technique has 53 revealed cell lineage [3], cell-type heterogeneities [4, 5], and distinct patterns of gene expression 54 [6] that cannot be identified by conventional bulk cell analysis. Despite the rapid growth and 55 56 maturation of the technique, many experimental and computational challenges remain [7]. Due to the limited amount of RNA extracted from each cell and various technical factors [8], e.g. 57 amplification bias and low RNA capture rate, scRNA-Seq data are very noisy and contain 58 frequent gene expression detection failures (i.e. dropout events [9]). Although several scRNA-59 Seq imputation methods such as MAGIC [10], scImpute [11], and Saver [12] have been 60

-3-

developed to improve analytical accuracy, over-processing of data can cause information loss,
and increase the lower bound of detection-error probability due to data processing inequality and
Fano's lemma in information theory [13] (see Methods). Moreover, the massive size of scRNASeq datasets demands extensive processing time, hindering the applicability of imputation
methods to ever-growing collections of scRNA-Seq data [14]. Together, these challenges
significantly hinder the progress of scRNA-Seq in its use as a technique and its application to
biological and biomedical research.

Traditional single-cell data processing methods typically perform cell-type identification 68 followed by subsequent DEG analysis [15-17]. However, there are major disadvantages with this 69 70 two-step method. First, cell-type identification or cell-clustering accuracy may significantly impact DEG analysis. Second, potential valuable information derived from DEG algorithms is 71 not used in cell-type identification. Here, we propose a generalized zero-inflated negative 72 73 binomial mixture model, "JOINT," that can perform probability-based cell-type discovery and 74 DEG analysis simultaneously without the need for imputation. The proposed model is an unsupervised learning problem which is solved by using the EM algorithm. Most published 75 studies do not provide test results for model validation, and the statistical distribution of single-76 cell data remains unclear. We show for the first time (by a statistical test) that the excessive zero-77 78 counts in scRNA-Seq data can be explained by this model.

Moreover, JOINT performs soft-clustering for cell-type discovery by computing the probability of cell identity for individual cells, where each cell can belong to multiple cell types with different probabilities. This is different from existing algorithms which typically perform hard-clustering where each cell can only belong to one cell type. JOINT identifies the optimal number of cell-types through Akaike Information Criterion (AIC) automatically rather than

-4-

84	specified empirically. All parameters in JOINT are calibrated automatically, without the need for
85	setting hyperparameters, e.g. number of cell-types. Existing clustering algorithms typically
86	perform log-transformation on the count data first, whereas JOINT uses the raw count data
87	directly. Therefore, potential biases introduced during data processing are greatly reduced. We
88	comprehensively evaluated the impact of dropout probability and tested the performance of
89	JOINT on cell-clustering and DEG analysis using simulated and real scRNA-Seq datasets. We
90	show that JOINT obtains better clustering performance on both simulated and real, large-scale
91	scRNA-Seq datasets when compared to existing algorithms.
92	We also leverage parallel computing methods in data processing: A Python package is
93	implemented and run on GPU using the TensorFlow deep learning framework's
94	(http://www.tensorflow.org/) low-level API to solve our unsupervised learning model. The
95	computational speed of the JOINT algorithm is 3,532 times faster when run on a GPU, versus a
96	Python NumPy implementation on CPU for a simulated dataset with 1,000 cells and 2,000 genes.
97	We use instructions from TensorFlow directly instead of high-level neural networks APIs such
98	as Keras ( <u>https://keras.io/</u> ). The Python package that we have developed is the first that can
99	perform cell-clustering and DEG analysis simultaneously on GPU, which dramatically
100	accelerates the computational speed for large-scale scRNA-Seq data analysis. Although not
101	required by JOINT for cell-type identification or DEG analysis, an imputation algorithm is
102	embedded for data visualization.
103	Finally, our DEG analysis algorithm directly applies soft-clustering results from JOINT,
104	rendering the ability to extract high quality cell-type information and perform accurate DEG
105	identification. Existing GPU-based imputation algorithms only use GPU in the imputation step

and still require standard cell-clustering and DEG pipeline in downstream data analysis, which

-5-

are typically performed on CPU. In contrast, our model does not require the imputation step and
can perform both cell-clustering and DEG analysis on GPU. Our study shows a new paradigm of
leveraging the use of GPU on large-scale scRNA-Seq data analysis. Overall, the JOINT
algorithm provides a more accurate, robust, and scalable method for analysis of large-scale
scRNA-Seq datasets. The package that we developed is generic and can be readily applied to aid
future advances in parallel computing-based single-cell algorithms.

113

#### 114 **RESULTS**

#### 115 Overview and Validation of the JOINT Algorithm

116 Existing bulk DEG analysis algorithms (e.g. DESeq2 [18]) and single-cell DEG analysis algorithms (e.g. MAST [19]) assume that cell-type is given, and DEG detection is performed 117 within these given cell-types. As such, cell-type accuracy significantly impacts DEG detection 118 and analysis. Additionally, parameters derived from DEG algorithms may provide useful 119 information for cell-type discovery. We investigate whether simultaneously performing cell-type 120 identification and downstream DEG model calibration benefits both processes. In the JOINT 121 algorithm, we consider the probability of observing count x follows a general mixture model. We 122 assume that each mixture component takes a generalized zero-inflated negative binomial model 123 with multiple negative binomial components (see Methods). Instead of performing hard-124 125 clustering for cell-type identification, where a given cell is clustered into a particular cell-type, we obtain the probability of individual cells belonging to each cell-type with JOINT. The 126 127 probability of observing count x from cell-type k and model parameters are calibrated jointly for 128 cell-type discovery and DEG analysis, rather than fixing cell-type first and estimating DEG parameters thereafter (Methods and Fig. 1a). For each cell-type k and gene g, our model extends 129

-6-

the current use of zero-inflated negative binomial distribution [20] by allowing multiple negative binomial components rather than one. Additionally, we derive an EM algorithm to calibrate all parameters in the zero-inflated negative binomial model for single-cell data automatically, which can also be used for arbitrary numbers of negative binomial components.

We first validated the model by testing whether it could explain the excessive zero-counts 134 in a real scRNA-Seq dataset. We chose the Zeisel dataset [21] and analyzed gene expression with 135 136 the "Oligodendrocyte" label provided in the dataset (see Methods). For each gene, we tested the performance of three JOINT variations: 1) negative binomial (Poisson-Gamma mixture), 2) zero-137 inflated negative binomial, and 3) zero-inflated negative binomial with two components. We 138 139 trained all three variations of the algorithm on GPU using TensorFlow, obtained predicted zerocount probability for each gene across all cells and compare the mean to the empirical zero-count 140 probability. Then, we tested if the predicted zero-count probability is significantly different than 141 the empirical value for each JOINT variation (see Methods). We found that p-values for the 142 comparisons were: p=1.58e<sup>-19</sup> for 1) *negative binomial*, p=0.057 for 2) *zero-inflated negative* 143 binomial, and p=1.12e<sup>-10</sup> for 3) zero-inflated negative binomial with two components. Since the 144 zero-count probability from 2) zero-inflated negative binomial model is not significantly 145 different than the empirical value, we concluded that this variation can recover the zero-count 146 147 probability. This finding provides the first statistical evidence that excessive zero-counts in scRNA-Seq data can be explained by a zero-inflated negative binomial distribution. In the rest of 148 the paper, we assume that gene expression follows the zero-inflated negative binomial 149 150 distribution (with one component), but arbitrary numbers of negative binomial components can 151 be selected and applied in the model for different single-cell datasets.

-7-

Next, as a sanity test, we examined whether the JOINT algorithm can converge to true
values. We generated a simulated dataset with two cell-types (clusters) and two genes as the
"ground truth" (see Methods). JOINT successfully converged to true values when we varied the
number of iterations, number of samples (cells), and dropout probabilities (Fig. 1b-1d and Fig.
S1-S3).

157

#### 158 Evaluation of Clustering Performance using Simulated Datasets

159 We next compared the clustering performance of JOINT to other algorithms using a simulated 160 dataset containing two cell-types and two genes (Fig. 2 and Table S1). We fixed the dropout probability at  $q_0=0.2$  and generated 5,000 cells (see Methods). For published algorithms, we 161 162 applied K-means clustering with 100 random initial points to the dataset and chose clustering results with the best Adjusted Rand Score for comparison. We compared the performance of 163 JOINT on the original non-imputed data, to K-means on the non-imputed and Saver [12] -164 imputed datasets (Fig. 2a-2h and Table S1). ScImpute [11] was not included since it cannot be 165 166 applied to 2-dimensional data. We demonstrated that JOINT obtained much higher clustering scores on the non-imputed data, than K-means on both the non-imputed and Saver-imputed 167 datasets. JOINT's performance also surpassed that of K-means on the original data without 168 169 dropout (Table S1). In this dataset, K-means performance was worse in log-transformed counts when compared to non-log-transformed data, suggesting log-transformation may lead to 170 information loss (Fig. 2f and 2g). In contrast, non-log-transformed raw data can be directly used 171 in the JOINT algorithm, minimizing potential bias and information loss. The JOINT algorithm 172 can also automatically optimize the number of clusters through AIC, rather than forcing a choice 173 from intuition. We ran the JOINT algorithm with the number of clusters K ranging from 1 to 5. 174

-8-

For each *K*, we randomly chose initial points, ran the proposed JOINT algorithm 10 times, and chose results with the highest likelihood. We found that the log likelihood did not increase when *K* was greater than 2, and both AIC and Bayesian Information Criterion (BIC) were minimized when K=2. Therefore, JOINT took K=2 as the optimal number of clusters, which precisely predicted the number of clusters in the simulated dataset (Fig. 2i-2k).

We further examined JOINT's performance on a more complex simulated dataset with 180 181 three cell-types, using parameters derived from published scRNA-Seq data to mimic real experimental settings (Methods and Fig. S4). We systematically examined the clustering 182 performance of JOINT at different dropout probabilities and DEG numbers. We evaluated the 183 184 performance of JOINT and other published algorithms at dropout probability  $q_0=0.1, 0.2$  and 0.3 and DEG number n=50, 100 and 150 (Fig. 3 and Fig. S5-S7). We generated 10 datasets for each 185 dropout probability and DEG number combination, and applied JOINT, Saver, and scImpute to 186 each dataset. We showed that JOINT obtained the highest Adjusted Rand Index score among all 187 188 algorithms tested, strongly suggesting its performance was superior over Saver and scImpute (Fig. 3a-3c and Fig. S6a-S6d). It is worth noting that although JOINT performs cell-type 189 identification without the need of imputation, it acquires the ability to impute for data 190 visualization (Methods, Fig. 3, and Fig. S5-S7). 191

Finally, we compared the clustering outputs from JOINT, Saver, and scImpute to the original dataset without dropout, to access the accuracy of performance. Since we used a simulated dataset, "true labels" without dropout were known. We correlated the clustering outputs to "true labels," and compared the correlation coefficients for the different algorithms. Higher correlation coefficients indicate better performance. We found that when we performed this correlation test at different dropout probabilities and DEG numbers, JOINT obtained higher

-9-

correlation coefficients than other imputation methods (Fig. 3d, 3e, and Fig. S6e). Overall, we
leveraged a simulated dataset with known cell-types to evaluate the performance of JOINT at
different dropout probabilities and DEG numbers. Since the simulated dataset was generated
using parameters derived from real scRNA-Seq data, we validated the JOINT algorithm in
conditions that mimic real experimental settings.

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204	Evaluation of Clustering Performance using Real, Large-scale scRNA-Seq Datasets
205	To futher evaluate JOINT's performance, we compared its clustering performance and
206	computing time to Saver and scImpute using real, large-scale scRNA-Seq datasets (Baron [22]
207	and Zeisel [21]). The cell-types identified by JOINT algorithm matched the published results
208	when applied to the Baron and Zeisel data (Fig. 4d and 4h). JOINT also obtained higher or
209	comparable Adjusted Rand Index, Jaccard Index, and Adjusted Mutual Information scores when
210	compared to Saver and scImpute methods (Fig. 4 and Table 1).
211	We then evaluated the computing time of JOINT compared to other imputation
212	algorithms. We found both the performance and speed of the JOINT algorithm was dramatically
213	accelerated over existing algorithms (Table 1). This is the first study that systematically
214	examined the performance and computing time of different imputation algorithms. The JOINT
215	algorithm functions as a useful parallel computing-based method for scalable scRNA-Seq
216	analysis. Since JOINT runs from an initial point, we also examined whether clustering
217	performance was improved by the EM algorithm through JOINT, or relied heavily on initial
218	conditions. We compared the JOINT-obtained clustering scores on the Zeisel dataset using
219	randomly selected initial points or those selected through K-means with and without the
220	application of EM algorithm. We demonstrated that the EM algorithm indeed improved the

-10-

clustering performance of JOINT when the initial points were either randomly selected or usingK-means (Fig. S8).

223

#### 224 Evaluation of JOINT Performance in DEG analysis

The JOINT algorithm also acquires the function of performing DEG analysis simultaneously 225 with cell-type identification. We evaluated JOINT's performance in DEG analysis using a 226 227 simulated dataset with 3 clusters from cells labeled "CA1 Pyramidal" from the Zeisel dataset 228 [21] (see Methods). We examined JOINT's performance in two conditions: true cell-type labels 229 as known or unknown. First, we assumed that all cell-types were known, and set the dropout probability to  $q_0=0.1, 0.2$ , and 0.3 for all cells and selected n=50, 100, and 150 DEG in the 230 231 simulated dataset. In real experimental settings, dropout probability is unlikely to be a set number across all cells. Therefore, we varied the dropout probability  $q_0$  by 0.05 for each cluster 232 (e.g. When  $q_{0,mean}$  for all cells=0.1, we obtained  $q_0$ =0.05, 0.1, and 0.15 for clusters 1, 2, and 3 233 respectively). The performance of JOINT and other published DEG analysis algorithms were 234 235 evaluated using the false/true positive rate relationship (Receiver Operating Characteristic (ROC) curve). DEG analysis results from cluster 1 and cluster 3 were then compared across algorithms 236 (Fig 5a-5d). When we used Area Under the Curve (AUC [23]) to compare the performance of 237 238 MAST [19], scDD [24], DESeq2 [18], and JOINT, we found that JOINT obtained higher AUC scores compared to other algorithms at different dropout probabilities and DEG numbers (Fig. 239 5a-5d). 240

Next, we considered the case where cell-type labels were unknown, but derived from a clustering algorithm. Since cell-types are unknown before analysis in real scRNA-Seq datasets, this test allows us to evaluate all algorithms in conditions similar to real experiments. For

-11-

published DEG analysis algorithms, we first performed K-means clustering and spectral 244 clustering on log(1+count), PCA on log(1+count) with 2 components, and PCA on log(1+count) 245 with components explaining 25% or 40% of variance on the simulated data. Cluster labels which 246 generate the highest Adjusted Rand Index scores were chosen for DEG analysis for published 247 methods. For JOINT, we initialized the algorithm with the same 8 conditions for fair 248 249 comparison. We want to emphasize that for existing DEG analysis methods, true cell labels must be known in order to compute Adjusted Rand Index scores. Since we opted to use the highest 250 251 Adjusted Rand Index scores for published algorithms, it is in fact, an overestimation of their 252 performance. In contrast for JOINT, we chose the clustering results that provided the highest likelihood for individual cells belonging to certain clusters, thus eliminating the need of knowing 253 true cell labels beforehand. Based on the clustering results from each algorithm, we identified 254 cell-types with the highest correlation with the original clusters 1 and 3, and performed DEG 255 analysis on these clusters. We compared AUC scores for MAST, scDD, DESeq2 and JOINT 256 257 algorithms. We found the JOINT algorithm obtained the best AUC scores among all the DEG analysis methods tested at different dropout probabilities (same dropout probability across all 258 cells) and DEG numbers (Fig 5e-5h). 259

Finally, we evaluated JOINT's performance in DEG analysis using a real, large-scale scRNA dataset. We analyzed a scRNA-Seq dataset GSE75748 [25] with both bulk and singlecell RNA-seq data on human embryonic stem cells (ESC) and definitive endoderm cells (DEC). This dataset includes four samples in H1 ESC, and two samples in DEC from bulk RNA-Seq; 212 cells in H1 ESC and 138 cells in DEC from scRNA-Seq. We used an R package (DESeq2) to identify DEG from bulk data and applied MAST, scDD, and DESeq2 to identify DEGs from the original scRNA-seq data or imputed data by Saver and scImpute. As DESeq2 requires non-

-12-

267	zero integer inputs, we rounded the imputed counts and added 1 for DEG analysis. We applied
268	different thresholds to False Discovery Rates (FDRs) of genes in bulk data to obtain a DEG list
269	as the reference for single-cell DEG analysis. Next, we compared AUC scores for JOINT and
270	other DEG analysis algorithms in combination with imputation methods. All algorithms that
271	were used for comparison include: MAST+Original, MAST+Saver, MAST+scImpute,
272	scDD+original, scDD+Saver, scDD+scImpute, DESeq2+Original, DESeq2+Saver,
273	DESeq2+scImpute, and JOINT. We found JOINT had superior performance over all other
274	existing imputation and DEG analysis algorithms that were tested (Fig. 5i).
275	We also systematically examined the computational time of JOINT. We compared the
276	computational time of one iteration in the EM algorithm between TensorFlow using GPU,
277	TensorFlow using CPU (run on compiled C code), and Python-based NumPy implementation
278	using CPU. We examined the scenario with 1,000 cells and 9 cell-types. We simulated the
279	dataset randomly and varied the number of genes from 1,000 to 2,500 (Fig. 5j). When the
280	number of genes is 2,000 (based on the number of highly differential genes used in Seurat
281	procedure), we found that TensorFlow run on GPU had a 35.6x speedup over TensorFlow run on
282	CPU, and a 3,532x speedup over NumPy run on CPU (Fig. 5j and Table S2). Overall, we
283	demonstrated that the performance of JOINT significantly improved both the accuracy and
284	efficiency of DEG analysis compared to current algorithms.

285

#### 286 **DISCUSSION**

We propose a mathematical algorithm, "JOINT," that performs cell-type discovery and DEGanalysis by parallel computing. Since there is no need for imputation, the potential for

289 information loss from data over-processing is minimized. Instead of assigning each cell into a

-13-

hard-cluster, this cell-type probability-based soft-clustering approach makes this algorithm more 290 accurate and robust. We validated the model extensively, and examined the performance of 291 292 JOINT on cell-type identification and DEG analysis using both simulated and real, large-scale scRNA-Seq datasets. Most published studies do not provide test results for model validation, and 293 the statistical distribution of single-cell data from these models is unclear. We show, for the first 294 295 time, that excessive zero-counts in real scRNA-Seq data can be explained by a properly trained zero-inflated negative binomial distribution. All parameters in JOINT are calibrated 296 297 automatically without needing to set any hyperparameters, such as the number of cell-types. 298 While existing clustering algorithms typically perform log-transformation on the count data first, our model uses the raw count data directly. Therefore, potential biases introduced during data 299 processing are greatly reduced. Moreover, when we evaluate the performance of JOINT on cell-300 type identification and DEG analysis, the joint-analysis feature of JOINT makes it more reliable 301 and efficient over existing algorithms that were tested. 302

303 We developed a Python package using the TensorFlow low-level API to train our model on GPU. The computational speed of the JOINT algorithm is 3,532 times faster when run on a 304 GPU versus a Python NumPy implementation on CPU for a simulated dataset. The Python package 305 306 we have developed is the first one that can perform cell-clustering and DEG analysis 307 simultaneously on GPU, which dramatically facilitates an increase in computing speed for largescale scRNA-Seq data analysis. The Python package is generic and can be applied to a generalized 308 zero-inflated negative binomial distribution with arbitrary number of negative binomial 309 310 components for different scRNA-Seq datasets.

In conclusion, JOINT can be readily applied to aid future advances in parallel computingbased single-cell algorithms. JOINT greatly improves the accuracy, scalability and speed of single-

-14-

cell data processing, making it a suitable candidate for future work involving scalable scRNA-Seqdata analysis.

315

#### 316 **METHODS**

#### 317 Over-processing of Data by Imputation May Cause Information Loss Due to Data

#### 318 **Processing Inequality and Fano's Lemma**

Let three random variables form the Markov chain  $X \to X' \to Y$ , implying that the conditional

distribution of Y depends only on X' and is conditionally independent of X. By data processing

inequality [13], the mutual information between *X* and *Y* is greater than or equal to that between X' and *Y*, i.e.

$$I(X;Y) \ge I(X';Y) \tag{1}$$

323 X is observed single-cell data, X' is imputed data, Y is decision variables, such as cell-types or

324 DEG. This equation indicates the information of data cannot be increased from data imputation.

Note that if we have a priori information *S* about genes or cell-types, we may have  $I(X; Y) \le I(X';$ 

- 326 Y|S, which indicates data imputation with a priori information may improve mutual information.
- 327 But even in this case, we still have  $I(X; Y|S) \ge I(X'; Y|S)$ .

328 From Fano's inequality, we have a lower bound on the detection-error probability (cell-

329 type mis-classification or DEG mis-detection)

$$p_e = Pr(\hat{Y} \neq Y) \ge \frac{H(Y) - I(X;Y) - 1}{\log(|Y|)}$$
 (2)

From data processing inequality, if processed data X' instead of un-processed data X is used, the right-hand side of equation (2) becomes bigger. Even though (2) is only a lower bound, data imputation increases the lower bound of error-detection. Therefore, performing data imputation 333 on observed data and performing subsequent analysis leads to information loss and an increase of

a lower bound on the detection-error probability. This indicates that there is an opportunity to

perform cell-type discovery and DEG analysis simultaneously to prevent such an information

336 loss.

337

#### 338 JOINT Algorithm

339 In the JOINT algorithm we consider a general mixture model

$$p(x) = \sum_{k=0}^{K-1} \pi_k f_k(x|\theta_k)$$

where *x* is observed count number, *k* is the number of cell-types,  $\pi_k$  is the probability of choosing cell-type *k* and  $f_k(x|\theta_k)$  is the probability of observing *x* given parameters  $\theta_k$  in cell-type *k*. Given *x* and  $\theta_k$ , we compute the posterior probability of observed counts *x* from cell-type *k* as

$$p(k|x) = \frac{\pi_k f_k(x|\theta_k)}{\sum_{\kappa=0}^{K-1} \pi_k f_\kappa(x|\theta_\kappa)}.$$

Rather than using hard-clustering methods where a given cell is clustered into a particular cell-343 type, we obtain the probability of individual cell belonging to each cell-type (Fig. 1a). If a cell 344 has non-zero probability p belonging to cell-type k, then it contributes accordingly (proportional 345 to p) to clustering and DEG analysis for cell-type k (Fig. 1a). Here, we assume that  $f_k(x|\theta_k)$  takes 346 a generalized zero-inflated negative binomial model with multiple negative binomial components 347  $q_{g,k,0}1_{x_g==0} + \sum_{l=1}^{L-1} q_{g,k,l} \int Gamma(\lambda_{g,k,l} | \alpha_{g,k,l}, \beta_{g,k,l}) Poisson(x_g | s_c \lambda_{g,k,l}) d\lambda_{g,k,l}$ where there are L components,  $q_{g,k,0}$  is the dropout probability for gene g in cell-type k,  $1_{x_q==0}$  is 348 1 when  $x_g=0$ , and otherwise 0.  $q_{g,k,l}$  is the probability that the observed count  $x_g$  is from the *l*-th 349 negative binomial component for gene g in cell-type k, and  $s_c$  is a cell level scaler. We choose 350 351 the same cell scaler as Seurat process which normalizes the library size to 10,000. The dropout probability  $q_{g,k,0}$  is the probability of observing zero-counts, regardless of the real expression 352

level of gene g. When the first dropout term is omitted and L=1, we obtain a <u>negative binomial</u>

354 *model*. When *L*=2, the model reduces to the *zero-inflated negative binomial model*. When *L*=3,

355 we obtain a <u>zero-inflated negative binomial model with two components</u>. Note that  $f_k(x|\theta_k)$  can be

also adapted and used for other models in DEG analysis.

To generate observed count x, we first draw a cell-type k from  $\pi$ , which determines a set 357 of parameters used for each gene in cell-type k. Then, we choose a negative binomial component 358 359 type *l* with probability  $q_{g,k,l}$ . When *l*=0, we set  $x_g=0$ , which corresponds to dropout and the process stops. When l > 0, we choose  $\alpha_{g,k,l}$  and  $\beta_{g,k,l}$  for each gene in cell-type k and generate a 360 Poisson intensity  $\lambda_{g,k,l}$ . Finally, we generate the observed count  $x_g$  from a Poisson distribution 361 362 with intensity  $\lambda_{g,k,l}$ . Given observed counts in a given cell  $x = [x_0, \dots, x_{G-l}]$ , we estimate  $\theta = \{\alpha_{g,k,l}, \dots, \alpha_{G-l}\}$  $\beta_{g,k,l}, q_{g,k,l}, \pi_k$  by maximizing the Probability Mass Function where we assume individual genes 363 obtain independent parameters  $\alpha_{g,k,l}$ ,  $\beta_{g,k,l}$ ,  $q_{g,k,l}$ . 364

$$p(\mathbf{x}|\pi_k, q_{g,k,l}, \alpha_{g,k,l}, \beta_{g,k,l}) = \sum_{k=0}^{K-1} \pi_k \prod_{g=0}^{G-1} \left( q_{g,k,0} \mathbf{1}_{x_g=0} + \sum_{l=1}^{L-1} q_{g,k,l} \int Gamma(\lambda_{g,k,l}|\alpha_{g,k,l}, \beta_{g,k,l}) Poisson(x_g|s_c\lambda_{g,k,l}) d\lambda_{g,k,l} \right)$$
365 We do not assume a constant dispersion across all genes but rather each gene has its own

366  $\alpha_{g,k,l}$  and  $\beta_{g,k,l}$ . The dropout probability  $q_{g,k,0}$  is optimized for each gene without assuming specific 367 dependence on the mean expression. Each cell-type has its own negative binomial distribution

- 368 rather than a single distribution shared across all cell-types. The mixture model is an
- unsupervised learning problem which is solved using the EM algorithm.

Algorithm 1: EM ALGORITHM1 initialize model parameters  $\alpha$ ,  $\beta$ , q,  $\pi$ ;2 while parameters not converged do3E-step: given  $\theta^{(t)} = (\alpha, \beta, q, \pi)$ , compute $Q_c(z) = p(z|\mathbf{x}_c; \theta)$ ,4where  $z = (k, l, \lambda)$  are latent variables.4M-step: update  $\theta$  by solving $\theta^{(t+1)} = \arg \max_{\theta} \sum_c \sum_z Q_c(z) \log p(z, \mathbf{x}_c; \theta)$ .5 end

The probability of *x* from cell-type *k* and negative binomial distribution parameters  $\alpha_{g,k,l}$ and  $\beta_{g,k,l}$  (also used for DEG analysis) are calibrated jointly, rather than fixing the cell-type first and estimating parameters for DEG analysis thereafter. Although usually challenging when run on CPU especially with big dataset, model calibration is successfully achieved when it is trained on GPU. All model training and testing was performed on a computer with Intel Xeon CPU E5-2686 v4 @ 2.30GHz with 62GB RAM and NVIDIA Tesla K80 GPU with 17GB memory.

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#### 377 Model Validation Using the Zeisel Dataset

We chose the Zeisel dataset [21] and analyzed the gene expression with the "Oligodendrocyte"
label provided in the dataset for model validation. Top and bottom 10% cells were removed
based on their library size. Genes that have non-zero expression between 30% and 90% were
chosen. This resulted in a dataset with 742 cells and 3,069 genes for model testing and
validation. For each gene, we tested the performance of three variations of the JOINT algorithm:
1) *negative binomial* (Poisson-Gamma mixture), 2) *zero-inflated negative binomial* (initial points)

-18-

were: dropout probability  $q_0=0.1$ ,  $\alpha=$ mean, and  $\beta=1$ ), 3) <u>zero-inflated negative binomial with two</u> <u>components</u> where one component started from  $\alpha=0.1$  and  $\beta=1$  (mimic a Poisson component with rate 0.1 from reference [23]) and the other one started from  $\alpha=$ mean and  $\beta=1$  in training. The initial probability  $q_0$  was set to 0.5 for the first and 0.4 for the second components. For the proposed generalized zero-inflated negative binomial model with multiple negative binomial components, the probability of getting zero-count is

$$q_{g,k,0} + \sum_{l=1}^{L-1} q_{g,k,l} \left( \frac{\beta_{g,k,l}}{\beta_{g,k,l} + s_c} \right)^{\alpha_{g,k,l}}$$

In order to test whether the three variations of JOINT algorithm can explain the zero-390 counts in the Zeisel dataset, we trained all three variations of the algorithm on GPU using 391 TensorFlow, obtained predicted zero-count probability  $\hat{p}_{c,g}^0$  for each gene g and cell c, then 392 calculated the mean across all cells for each gene  $\hat{p}_g^0 = \frac{1}{c} \sum \hat{p}_{c,g}^0$ . We compared  $\hat{p}_g^0$  to the 393 empirical zero-count probability for each gene  $\bar{p}_{g}^{0}$  by counting the number of cells with zero-394 count (for this gene), divided by the total number of cells. Then, we performed two-sided student 395 t-tests with the null hypothesis that  $\hat{p}_g^0 - \bar{p}_g^0$  has mean 0, to examine whether each variation of 396 the model can recover the zero-count probability. We found that p-values were:  $p=1.58e^{-19}$  for 397 negative binomial, p=0.057 for zero-inflated negative binomial, and p=1.12e<sup>-10</sup> for zero-inflated 398 negative binomial with two components. Since we could not reject the null hypothesis (i.e. 399 400 predicted zero-count probability is the same as the empirical estimate at 95% confidence level), we concluded that the zero-inflated negative binomial model can recover the zero-count 401 probability. Although model 3 subsumes model 2, the EM algorithm may converge to a 402 403 suboptimal local optimum when model 3 is initialized as in Methods. 404

#### 405 Generation of a Simulated Dataset with Two Genes and Two Cell-types

-19-

406 Simulation set up: In order to validate and test the clustering performance of the model (Fig. 1b-

- 407 1d, Fig. 2, Fig. S1-S3 and Table S1), we generated a simulated dataset with two genes and two
- 408 cell-types (clusters) as the "ground truth." To set up the simulation, we chose  $\pi = \{0.4, 0.6\}$ ,
- 409  $q_{g,k,0}=0.2, q_{g,k,1}=0.8$ , and  $\beta_{g,k,1}=1.0$ ; first cluster  $\alpha_{0,0,1}=10$  and  $\alpha_{1,0,1}=5$ ; second cluster  $\alpha_{0,1,1}=30$  and 410  $\alpha_{1,1,1}=20$ .
- 411 *Convergence of the model with iterations:* We generated 10,000 samples from the mixture model
- using parameters described above. In the EM algorithm, we chose initial values  $\pi = \{0.5, 0.5\}$ ,
- 413  $q_{g,k,0}=0.1, q_{g,k,l}=0.9$ , and  $\beta_{g,k,l}=1.0$ ; first cluster  $\alpha_{0,0,l}=8$  and  $\alpha_{1,0,l}=8$ ; second cluster  $\alpha_{0,l,l}=25$  and
- 414  $\alpha_{1,1,1}$ =25. The JOINT algorithm converged after 30 iterations (Fig. 1b and Fig. S1).
- 415 Convergence of the model with number of samples: For a given number of samples, we randomly 416 generated 50 datasets and applied JOINT on each dataset for statistics. As the number of samples 417 increased, we found that the EM estimate converged to the actual values with smaller variances 418 (Fig. 1c and Fig. S2). This agrees with the fact that Maximum Likelihood (ML) estimates 419 converge almost surely to true values asymptotically when the number of samples goes to 420 infinity [26].
- 421 *Convergence of the model with dropout probability:* We fixed the number of samples as 1,000 422 and varied the dropout probability  $q_{g,k,0}$  from 0.1 to 0.5 with step size of 0.1. At each dropout 423 probability, we generated 50 datasets and ran JOINT on each dataset to test the convergence 424 (Fig. 1d and Fig. S3).

425

#### 426 Generation of a Simulated Dataset with Three Cell-types using Zeisel Data

We simulated a scRNA-Seq dataset with 3 cell-types (Fig. 3 and Fig. S5-S7). We trained JOINT 427 on cells with the "CA1 Pyramidal" label in the Zeisel dataset [21] for each gene using the EM 428 algorithm. First, we chose cells with >10,000 library size and genes with non-zero-counts in at 429 least 40% of cells. Then, we trained the JOINT algorithm on the 3,529 genes and 834 cells that 430 were selected. Next, we randomly chose 1,000 genes without replacement from the selected 431 432 3,529 genes and generated three cell-types (1,200 cells in total). We randomly generated gene counts for 400 cells in each cell-type. In order to generate cells with different DEG numbers, we 433 randomly selected n genes (n=50, 100 and 150) from the chosen 1,000 genes without 434 435 replacement and set the mean expression of these genes 1.5 times higher in one cluster than in the other two (1.5 is the median of the gene expression ratio between cells with "CA1 436 Pyramidal" and "Oligodendrocytes" labels in the dataset (Fig. S4)). 437

438

439 Evaluation of Clustering Performance

440 Evaluation of clustering performance using simulated data sets with three genes and three

441 *clusters:* We assumed the number of cell-types *K*=3 was known in all algorithms. We performed K-means clustering and spectral clustering on imputed counts from published algorithms with 442 the following transformations: log(1+count), PCA on log(1+count) with 2 components, PCA on 443 log(1+count) with components explaining 25% or 40% of variance. Since we do not know the 444 transformation required to achieve best performance for published imputation algorithms, we 445 tested all 8 transformations for each, and chose the one with the best score for comparison. We 446 also ran the JOINT algorithm (initialized with the same 8 conditions) using original unimputed 447 counts, and chose the one with the highest likelihood as the final solution. In order to obtain 448 clustering scores for JOINT, we assigned each individual cell to the cell-type with the highest 449

-21-

posterior probability, converting soft-clustering into hard-clustering results. Although Seurat 450 process [15] can also be used for clustering, different parameters must be chosen for each 451 individual dataset in order to achieve cluster number K=3. Given that the performance of 452 multiple algorithms at different dropout probabilities and DEG numbers needed to be tested 453 extensively, K-means clustering method was used to simplify the process. It is also worth 454 455 emphasizing that for data mapping and visualization in lower dimensional space, we applied the PCA from the original data without dropout, to the imputed data from published algorithms and 456 457 data from JOINT, so that all data were transformed with the same projection from higher 458 dimensional space to 2-dimensional space (Fig. 3, Fig. S6, and S7). Mapping to 2-dimensional space allows us to compare these different algorithms by inferring aspects of their relative 459 positions in the original higher dimensional space. This is different than published work where 460 PCA is performed for each individual dataset [11], which makes data incomparable following 461 transformation. Although the simulated dataset may not have the same distribution as the original 462 463 data, the performance of different algorithms in various conditions can be investigated. Evaluation of clustering performance using real, large-scale scRNA-Seq datasets: We first 464 applied Saver and scImpute algorithms to Baron and Zeisel datasets with default parameters for 465 466 imputation. Then, we applied standard Seurat process with default parameters to the imputed 467 data using 2,000 highly expressed genes and cluster number K=9 and 9 for each dataset. The 468 number of PCA components in Seurat [15] was set to 25 and 45 (from the elbow method [15, 27]) for Baron and Zeisel datasets respectively. Finally, we applied the JOINT algorithm to both 469

470 datasets.

471 *Correlation analysis (cell and gene correlation):* We consider cell to cell correlation and gene to 472 gene correlation. For cell to cell correlation, let  $x_c = [x_{c,1}, \dots, x_{c,G}]^T$  be a vector of counts without

-22-

473 dropout for cell *c* and  $y_c = [y_{c,1}, \ldots, y_{c,G}]^T$  be the corresponding vector of imputed counts. We

474 compute the Pearson correlation between  $x_c$  and  $y_c$  as

$$\rho_c = pearsonr(\mathbf{x}_c, \mathbf{y}_c)$$

475 The cell to cell correlation is defined as the average of  $\rho_c$  across all cells, i.e.,

$$\rho_{cell} = \frac{1}{C} \sum_{c=1}^{C} \rho_c$$

476 Similarly,  $x_g = [x_{1,g}, \ldots, x_{C,g}]^T$  be a vector of counts without dropout for gene g and  $y_c = [y_{1,g}, \ldots, y_{C,g}]^T$ 

- 477  $y_{C,g}^{T}$  be the corresponding vector of imputed counts. We compute the Pearson correlation
- 478 between  $x_g$  and  $y_g$  as

$$\rho_g = pearsonr(\mathbf{x}_g, \mathbf{y}_g)$$

479 The gene to gene correlation is defined as the average of  $\rho_g$  across all gene

$$\rho_{gene} = rac{1}{G}\sum_{g=1}^G 
ho_g$$

480

#### 481 Imputation Algorithm for Data Visualization

We impute the observed counts directly. If the observed count is non-zero, we treat it as it is and 482 do not perform imputation. If the observed count is zero, we impute it based on the posterior 483 mean calculated from the JOINT algorithm. Consider a simple case in which we only have one 484 cluster K=1, one negative binomial component L=2, and the observed count is 0. If the observed 485 count is purely from the negative binomial component, the observed count 0 is the true count 486 (the true expression is 0). If the observed count 0 is purely from the zero component, the best 487 estimate in this case is the mean from negative binomial component which we assume is 5. If the 488 probability that the 0 count is from the zero component  $q_0=0.2$ , the probability from the negative 489 binomial component 1- $q_0=0.8$ , and the mean of negative binomial component is 5, then the mean 490

of the count imputed for given observed 0 is 0.2\*5+0.8\*0=1. We apply the idea formally, given observed count  $x_c$  in cell c, we first compute the posterior probability that c is from type k as  $n(k|\mathbf{x}_c) = \frac{\pi_k \prod_g \sum_l q_{g,k,l} h(\mathbf{x}_{c,g} | \theta_{g,k,l})}{\pi_k \prod_g \sum_l q_{g,k,l} h(\mathbf{x}_{c,g} | \theta_{g,k,l})}$ 

$$p(k|\mathbf{x}_c) = \frac{\pi_k \prod_g \sum_l q_{g,k,l'} (x_{c,g}|\theta_{g,k,l'})}{\sum_{\kappa=0}^{K-1} \pi_k \prod_g \sum_{l'} q_{g,\kappa,l'} h(x_{c,g}|\theta_{g,\kappa,l'})}$$

493 where

$$h(x_{c,g}|\alpha_{g,k,l},\beta_{g,k,l}) = \begin{cases} \int Gamma(\lambda_{g,k,l}|\alpha_{g,k,l},\beta_{g,k,l})Poisson(x_{c,g}|s_c\lambda_{g,k,l})d\lambda_{g,k,l}, & l > 0\\ 1, & l = 0 \end{cases}$$

494 Given  $x_{g,c}$  for gene g and cell-type k, the probability of  $x_{g,c}$  from the l-th negative binomial 495 component is

$$p(l|k, x_{g,c}) = \frac{q_{g,k,l}h(x_{c,g}|\theta_{g,k,l})}{\sum_{l'} q_{g,\kappa,l'}h(x_{c,g}|\theta_{g,\kappa,l'})}$$

496 The mean of each component l is  $s_c m_{g,k,l}$  where

$$m_{g,k,l} = \begin{cases} \frac{\alpha_{g,k,l}}{\beta_{g,k,l}}, & l > 0\\ 0, & l = 0 \end{cases}$$

With probability  $1-p(0|k, x_{g,c})$  the observed 0 is from a negative binomial component and we do not need imputation in this case. With probability  $p(0|k, x_{g,c})$  the observed count is from dropout events and we use the mean expression (conditional on this count is truly expressed) as the best estimate for imputation. The probability of *l*>0 conditional on this count is truly expressed is

$$p(l|k, x_{g,c}, expressed) = \frac{p(l|k, x_{g,c})p(expressed|k, x_{g,c}, l)}{p(expressed|k, x_{g,c})} = \frac{p(l|k, x_{g,c})}{p(expressed|k, x_{g,c})} = \frac{p(l|k, x_{g,c})}{1 - p(0|k, x_{g,c})}$$

501 We thus have the imputation value as

$$\sum_{k} p(k|\mathbf{x}_{c})(1-p(0|k,x_{g,c})) * 0 + p(0|k,x_{g,c}) \sum_{l>0} \frac{p(l|k,x_{g,c})}{1-p(0|k,x_{g,c})} s_{c} m_{g,k,l} = s_{c} \sum_{k} p(k|\mathbf{x}_{c}) \frac{p(0|k,x_{g,c})}{1-p(0|k,x_{g,c})} \sum_{l>0} p(l|k,x_{g,c}) m_{g,k,l} = s_{c} \sum_{k} p(k|k,x_{g,c}) m_{g,k,l} = s_{c} \sum_{k} p(k|k,x_{g,c}) \sum_{l>0} p(k|k,x_{g,c}) m_{g,k,l} = s_{c} \sum_{k} p(k|k,x_{g,c}) m_{g,k,l}$$

502

#### 503 **DEG Analysis**

We apply the Wald test [28] for DEG analysis by directly estimating the mean and the variance of expression conditional on that gene is expressed (or no dropout) for cell-type k. Given  $p(k|x_c)$  and  $p(l=0|k, x_{c,g})$ , let  $w_{c,k}=p(k|x_c)$  and  $v_{c,g,k}=1-p(l=0|k, x_{c,g})$ , where  $v_{c,g,k}$  is the probability that the observed zero-count is from a negative binomial component. We find the mean by minimizing

$$\sum_{c,x_{c,g}>0} w_{c,k} |x_{c,g} - m_{g,k}|^2 + \sum_{c,x_{c,g}==0} w_{c,k} v_{c,g,k} |x_{c,g} - m_{g,k}|^2.$$

508 We obtain

$$E(x_{c,g}|k, expressed) = m_{g,k} = \frac{\sum_{c,x_{c,g}>0} w_{c,k} x_{c,g}}{\sum_{c,x_{c,g}>0} w_{c,k} + \sum_{c,x_{c,g}=0} w_{c,k} v_{c,g,k}}$$

which is a weighted average with weight the probability of the observed count that is expressed
in cell-type k. Similarly, we compute E(x<sup>2</sup><sub>c,g</sub>|k) and obtain the variance as
σ<sup>2</sup>(x<sub>c,g</sub>|k) = E(x<sup>2</sup><sub>c,g</sub>|k) - E<sup>2</sup>(x<sub>c,g</sub>|k).
Wald test [28] is used with the estimated mean and variance. After model training, it requires

simple arithmetic operations to compute the mean and variance for Wald test. The Wald test p-512 513 values are adjusted using the Benjamini and Hochberg method [29]. As hard-clustering is a special case of soft-clustering with  $p(k|x_c) \in \{0, 1\}$ , all the proposed DEG algorithms can be 514 readily applied to hard-clustering as well. We are aware that we can use Fisher information 515 matrix to estimate the variance of MLE estimate. However, although a closed-form of Fisher 516 information matrix can be derived, we find the matrix is not always positive semidefinite for real 517 scRNA-Seq data. Therefore, the MLE estimate method cannot be used directly to identify the 518 variance of the EM algorithm. We can also use the likelihood-ratio test. However, it requires 519

training the JOINT multiple times, which is computational expensive.

521

#### 522 **DECLARATIONS**

#### 523 Ethics Approval and Consent to Participate

524 Not Applicable.

#### 525

-25-

526	Consent for Publication
527	Not Applicable.
528	
529	Availability of Data and Materials
530	Saver 1.1.2 was used in this study. Saver software can be found at
531	https://github.com/mohuangx/SAVER. ScImpute 0.0.9 was used in this study. ScImpute software
532	can be found at <u>https://github.com/Vivianstats/scImpute</u> . Seurat 3.1.4 was used in this study.
533	Seurat software can be found at <u>https://satijalab.org/seurat/</u> . Three published scRNA-Seq datasets
534	are used in this study: Baron (GSM2230757), Zeisel ( <u>http://linnarssonlab.org/cortex/</u> ), and Chu
535	(GSE75748). JOINT code can be found at <u>https://github.com/wanglab-georgetown/JOINT</u> .
536	
537	Competing Interests
538	The authors declare no competing interests.
539	
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544	

### 545 Authors' Contributions

546	T.W. envisioned and	designed the	e project. T.	C. implemented	the project and	conducted the
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547 analysis. T.C. and T.W. wrote the manuscript.

548

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- 554
- 555

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639		

#### 641 FIGURE LEGENDS

#### Fig. 1: Overview and convergence tests for the JOINT algorithm.

- 643 (a) Workflow of the JOINT procedure. Soft-clustering, parameter optimization and DEG
- analysis are performed simultaneously in JOINT. Probability-based soft-clustering for cell-type
- 645 identification and DEG analysis are demonstrated in the insets. (b) Convergence of  $\pi_k$  (*k*=1),
- 646  $q_{g,k,l}(g=0, k=0, \text{ and } l=1), \alpha_{g,k,l}(g=0, k=1, \text{ and } l=1), \text{ and } \beta_{g,k,l}(g=1, k=0, \text{ and } l=1) \text{ to true values}$
- 647 with iterations. (c) Convergence of  $\pi_1$ ,  $q_{0,0,1}$ ,  $\alpha_{0,1,1}$ , and  $\beta_{1,0,1}$  to true values with the number of
- 648 samples. (d) Convergence of  $\pi_1$ ,  $q_{0,0,1}$ ,  $\alpha_{0,1,1}$ , and  $\beta_{1,0,1}$  to true values with dropout probabilities.
- 649 True values are indicated by blue lines. Error bars in (c) (d) indicate the full range of data

650 variation.

651

#### **Fig. 2: Validation of JOINT's clustering performance.**

plot shows posterior probability (z-axis) for each cell (red dots) belonging to cell-type 1. 655 Expression levels of gene 1 (Dimension 1, Dim 1) and gene 2 (Dimension 2, Dim 2) are shown 656 on the x- and y-axis. (b) Surface plot shows the probability for individual cells belonging to cell-657 type 1 (hot color) and 2 (cold color). (c) - (h) Comparison of the clustering performance of 658 659 different algorithms. (c) Original dataset without dropout (True Labels). (d) Observed dataset with 0.2 dropout probability. (e) Cell-clustering by JOINT on the dataset with 0.2 dropout 660 probability. (f) Cell-clustering by K-means on non-log data with 0.2 dropout probability. (g) 661 662 Cell-clustering by K-means on log-transformed data with 0.2 dropout probability. (h) Cellclustering by K-mean on Saver-imputed data (non-log) with 0.2 dropout probability. Individual 663 cells in clusters 1 and 2 are shown in red and blue, respectively. (i) - (k) The JOINT algorithm 664 determines cell-cluster numbers automatically by likelihood (i), AIC (j), and BIC (k) tests. 665

(a) Cell-clustering by JOINT on a simulated dataset with two cell-types and two genes. Scatter

666

654

# Fig. 3: Comparison of clustering performance of different algorithms at various dropout probabilities and DEG numbers.

671 (dropout probability is set to 0.3 and DEG number set to 150). Original data with no dropout is

(a) Cell-clustering by JOINT, Saver, and scImpute on a simulated dataset with three clusters

shown on the left. Adjusted Rand Index for each algorithm is shown. K-means clustering method

673 is used for published imputation algorithms. Imputation algorithm in JOINT is used for data

visualization. For datasets with dropout, we applied the PCA from the original dataset without

dropout to get the 2-dimensional plot. (b) - (c) Cell-clustering scores are compared for JOINT,

676 Saver, and scImpute algorithms at different dropout probabilities on a dataset with 150 DEG (b)

and 50 DEG (c). (d) - (e) Correlation coefficients of cell-clustering results from JOINT, Saver,

and scImpute to original "true labels" are averaged across all genes (Gene Correlation) or cells

679 (Cell Correlation) at different dropout probabilities. Correlation coefficients generated from a

dataset with 150 DEG (d) and 50 DEG (e) are shown.

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# Fig. 4: Evaluation of JOINT's clustering performance with real, large-scale scRNA-Seqdatasets.

- 685 (a) (d) Cell-clustering and t-SNE visualization of the Barron dataset. Cell-clustering from raw
- data (a), Saver-imputed data (b), scImpute-imputed data (c), and JOINT (d) are shown.
- 687 Imputation algorithm in JOINT is used to visualize cell-clustering results. Adjusted Rand Index
- 688 scores are shown for all algorithms. (e) (h) Cell-clustering and t-SNE visualization of the Zeisel
- dataset. Cell-clustering from the raw data (e), Saver-imputed data (f), scImpute-imputed data (g),
- and JOINT (h) are shown. Imputation algorithm in JOINT is used to visualize cell-clustering
- results. Adjusted Rand Index scores are shown for all algorithms.

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#### **Fig. 5: Evaluation of JOINT's performance in DEG analysis.**

(a) - (d) Comparison of the performance of DEG analysis algorithms when cell labels are known 695 and different dropout probabilities are assigned to each cell-cluster. AUC scores for MAST, 696 scDD, DESeq2, and JOINT when different dropout probabilities are assigned to each cell-cluster 697 in datasets with 50 DEG (a), 100 DEG (b) and 150 DEG (c) are shown. (d) ROC curves for 698 MAST, scDD, DESeq2, and JOINT when mean dropout probability for all cells is set to 0.1 699 700 (dropout probability varies by 0.05 for each cell-cluster) and DEG number is set to 150. (e) - (h) Comparison of the performance of different DEG analysis algorithms when cell labels are 701 702 unknown and the same dropout probability is assigned to all cells. AUC scores for MAST, scDD, 703 DESeq2, and JOINT when the dropout probability is set to the same value for all cells in datasets with 50 DEG (e), 100 DEG (f) and 150 DEG (g) are shown. (h) ROC curves for MAST, scDD, 704 DESeq2, and JOINT when mean dropout probability for all cells is set to 0.1 and DEG number is 705 706 set to 150. (i) AUC curves of DEG analysis algorithms in combination with imputation methods and JOINT are shown. (j) Computing time of one iteration of the JOINT EM algorithm when run 707 by TensorFlow using GPU, TensorFlow using CPU (run on compiled C code), and Python-based 708 NumPy implementation using CPU. Computing time is tested for different numbers of genes. 709

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- 712 Table 1: Comparison of clustering performance and computing time for JOINT and
- 713 published imputation algorithms on real scRNA-Seq datasets.

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## Table 1

Performance Scores	Raw	Saver	scImpute	JOINT		
Baron Dataset						
Adjusted Rand Index	0.64	0.63	0.43	0.95		
Jaccard Index	0.55	0.53	0.34	0.92		
Adjusted Mutual Info	0.79	0.76 0.64		0.89		
Zeisel Dataset						
Adjusted Rand Index	0.67	0.69	0.45	0.67		
Jaccard Index	0.57	0.59	0.35	0.57		
Adjusted Mutual Info	0.63	0.63	0.56	0.65		

Computing Time (s)	Saver	scImpute	JOINT
Baron Dataset	4,777	1,010	528
Zeisel Dataset	18,036	3,440	836